What is claimed is:

- 1. A polymethylaluminoxane preparation generated by thermal decomposition of an alkylaluminum compound having an aluminum-oxygen-carbon bond, the alkylaluminum compound being generated by a reaction between trimethylaluminum and an oxygen-containing organic compound, wherein:
- (i) the oxygen-containing organic compound reacting with trimethylaluminum is an aliphatic or aromatic carboxylic acid represented by the general formula (I),
- 10 R^1 -(COOH)_n (I)

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(wherein R¹ represents a hydrocarbon group of C1-C20 straight or branched alkyl groups, alkenyl groups or aryl groups, and n represents an integer of 1 to 5);

- (ii) a mole fraction of methyl groups originating from 15 aluminoxane part, relative to the total moles of methyl groups existing in the generated polymethylaluminoxane preparation is not more than 26 mol%; and
 - (iii) the generated polymethylaluminoxane preparation has a viscosity of not more than 2.1 \times 10⁻³ Pa•sec at 40°C.
- 20 2. The polymethylaluminoxane preparation according to claim 1, wherein

the oxygen-containing organic compound represented by the general formula (I) is benzoic acid.

3. The polymethylaluminoxane preparation according to claim 1, wherein

the oxygen-containing organic compound represented by the general formula (I) is toluic acid.

4. A method of producing a polymethylaluminoxane preparation having a mole fraction of methyl groups originating from aluminoxane part, relative to the total moles of methyl groups of not more than 26 mol% and a viscosity of not more than 2.1×10^{-3} Pa•sec at 40°C, the method comprising the steps of:

causing trimethylaluminum to react with an oxygen
10 containing organic compound represented by the general formula

(I),

 R^1 -(COOH)_n (I)

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(wherein R¹ represents a hydrocarbon group of C1-C20 straight or branched alkyl groups, alkenyl groups or aryl groups, and n represents an integer of 1 to 5) to form an alkylaluminum compound having an aluminum-oxygen-carbon bond; and

thermally decomposing the alkylaluminum compound,

wherein a ratio between a mole number of trimethylaluminum and a mole number of oxygen in the oxygen-containing compound represented by the general formula (I) is in the range of 1.25 to 1.40 : 1.

5. The method of producing a polymethylaluminoxane preparation according to claim 4, wherein

the thermal decomposition is conducted in the absence of 25 a Lewis acid compound in production of the polymethylaluminoxane preparation.

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6. The method of producing a polymethylaluminoxane preparation according to claim 4 or 5, wherein

the oxygen-containing organic compound represented by the general formula (I) is benzoic acid.

- 7. The method of producing a polymethylaluminoxane preparation according to claim 4 or 5, wherein the oxygen-containing organic compound represented by the general formula (I) is toluic acid.
- 8. A polymerization catalyst for olefins, comprising as catalytic components:

a transition metal compound represented by the general formula (II),

 $MR^5R^6R^7R^8$ (II)

(wherein M represents a transition metal element, and R⁵, R⁶, R⁷, and R⁸ represent organic groups that form together a cycloalkadienyl backbone, such as an alkyl group, an alkoxy group, an aryloxy group, an alkylsilyl group, an alkylamide group, an alkylimide group, an alkylimino group, or a halogen atom); and

the polymethylaluminoxane preparation according to any one of claims 1 to 3.

9. A method of polymerizing olefins using the polymerization catalyst according to claim 8.